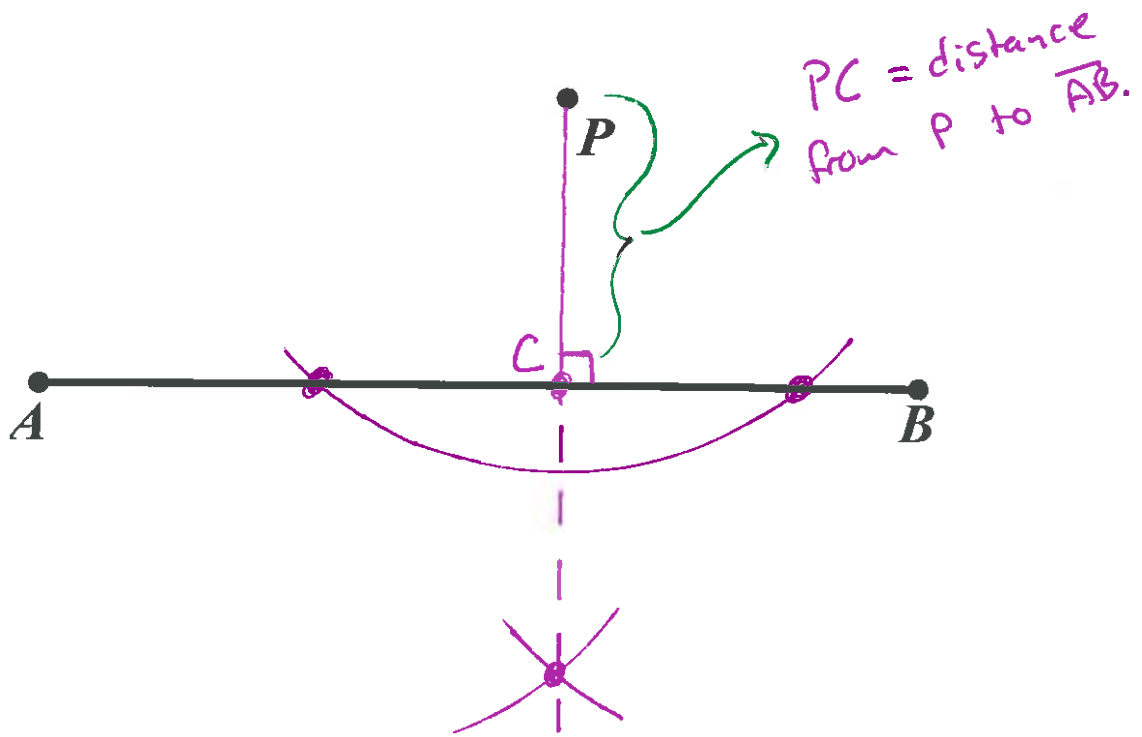


Using a compass and straight edge, construct a line perpendicular to  $\overline{AB}$  through point P.



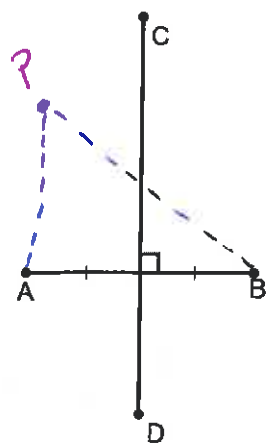
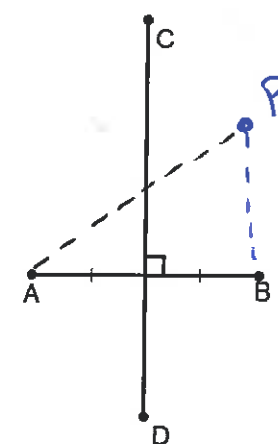
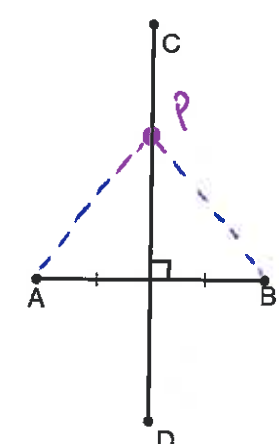
**Definition:** The distance from a point (P) to a line ( $\overline{AB}$ ) is...

the length of the segment that is  $\perp$  to the line  
from the point.

## Perpendicular Bisector Theorem

Perpendicular bisector.

In each picture  $\overline{CD}$  is the  $\perp$  bisector of  $\overline{AB}$ . How do AP and BP compare?

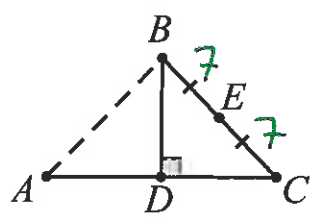
Picture 1	Picture 2	Picture 3
		
$AP < BP$	$AP > BP$	$AP = BP$

**Theorem:** A point on the  $\perp$  bisector of a segment is equidistant to the endpoints of the segment.

**Converse:** A point equidistant to the endpoints of a segment is on the  $\perp$  bisector of the segment.

**Example:**  $\overline{BD}$  is the perpendicular bisector of  $\overline{AC}$ .  $\rightarrow \overline{AB} \cong \overline{BC}$   
 E is the midpoint of  $\overline{BC}$   
 $EC = 7$

Find  $\overline{AB}$

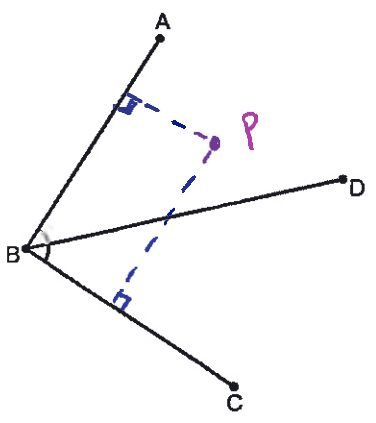
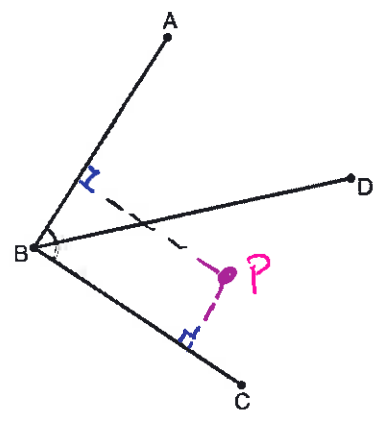
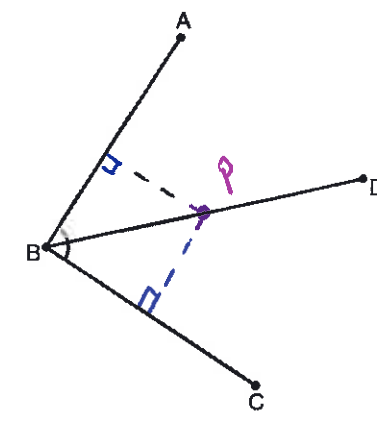


$$\begin{aligned}
 AB &= BC \\
 &= BE + EC \\
 &= 7 + 7 \\
 &= 14
 \end{aligned}$$

angle bisector

## Angle Bisector Theorem

In each picture  $\overline{BD}$  bisects  $\angle ABC$ . Point P is closest to which side of  $\angle ABC$ ?

Picture 1	Picture 2	Picture 3
		
P is closest to: <u>AB</u>	P is closest to: <u>BC</u>	P is closest to: neither (it's equidistant)

**Theorem:** A point on the angle bisector is equidistant to the sides of the angle.

**Converse:** A point equidistant to the sides of an angle is on the angle bisector.

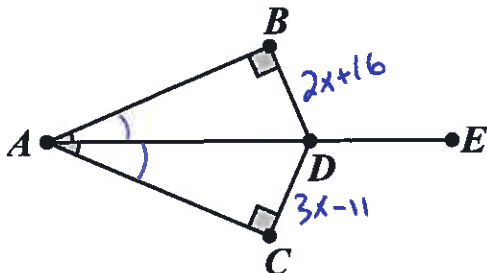
**Example:**

Given:  $\overline{AD}$  bisects  $\angle BAC$

$$BD = 2x + 16$$

$$CD = 3x - 11$$

Find x.



$$BD = CD$$

$$2x + 16 = 3x - 11$$

$$27 = x$$